Mauricio Romero



Introduction

Elasticities

Monopoly

Price discrimination

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Firm is faced a problem like the following:

$$\max_{K,L} p_x f_x(L,K) - wL - rK.$$

The firm's choice of L and K does not affect the prices p, w, r

This is called price-taking behavior

Justified if the the market is composed of many small firms

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In many markets there is a single firm

Since supply is completely controlled by the firm, it can use this in its favor

Profit maximization condition,

$$\max_{K,L} pf_{X}(K,L) - wL - rK.$$

► If

$$c(x) = \min_{K,L} wL + rK$$
 such that $f_x(K, L) = x$

then the above is equivalent to:

$$\max_{x} px - c(x).$$

▶ When firm controls supply, then:

$$\max_{x} \mathbf{p}(\mathbf{x}) x - c(x)$$

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Consumers willingness to pay is given by the demand function

\blacktriangleright p(x) is the **demand** function

▶ We can also represent the problem as:

$$\max_p pq(p) - c(q(p))$$

• q(p) is the inverse demand function

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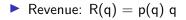
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• Revenue: R(q) = p(q) q

$$rac{dR}{dq} = p(q) + qrac{dp}{dq}(q) = p(q)\left(1 + rac{1}{arepsilon_{q,p}}
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 $\triangleright \ \varepsilon_{q,p}$ is the elasticity of demand with respect to price

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• If $\varepsilon_{q,p} \in (-1,0)$, the demand is *inelastic*

An increase in price leads a small decrease in demand

An increase in quantity leads to a big decrease in price

▶ If
$$\varepsilon_{q,p} < -1$$
, then demand is *elastic*

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What kind of demand functions have constant elasticities of demand with respect to price?

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$$rac{dq}{dp}rac{p}{q}=\kappa<0.$$

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$$\frac{dq}{dp}\frac{p}{q} = \kappa < 0.$$

$$rac{1}{q}rac{dq}{dp} = \kappa rac{1}{p} \Longrightarrow rac{d}{dp}\log q(p) = rac{d}{dp}\log p^\kappa.$$

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By the fundamental theorem of calculus:

$$\log q(p) = C + \log p^{\kappa}.$$

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•
$$q(p) = e^{C}p^{\kappa}$$
 or $q(p) = Ap^{\kappa}$ for some A.

Whenever the demand function has constant elasticity $\boldsymbol{\kappa}$

•
$$q(p)Ap^{\kappa}$$
 for some $A > 0$.

Equivalently,

$$p(q) = \left(rac{q}{A}
ight)^{1/\kappa}$$

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► The first order condition tells us:

$$rac{dR}{dq} = rac{dc}{dq} \Longrightarrow p(q) \left(1 + rac{1}{arepsilon_{q,p}}
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This implies

$$1+\frac{1}{\varepsilon_{\boldsymbol{q},\boldsymbol{p}}}>0 \Longleftrightarrow \varepsilon_{\boldsymbol{q},\boldsymbol{p}}<-1.$$

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$$1+rac{1}{arepsilon_{m{q},m{p}}}>0 \Longleftrightarrow arepsilon_{m{q},m{p}}<-1.$$

 A monopoly firm always produces at a point where demand is elastic

$$1+rac{1}{arepsilon_{q,p}}>0 \Longleftrightarrow arepsilon_{q,p}<-1.$$

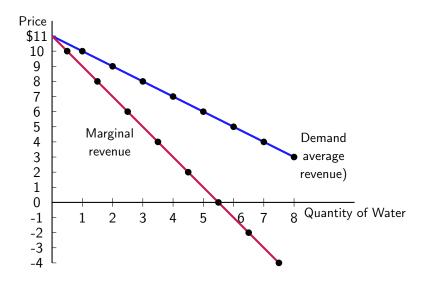
- A monopoly firm always produces at a point where demand is elastic
- If the firm produced at a point where demand was inelastic

• At such a point
$$\frac{dR}{dq} < 0$$

By reducing quantity (or raising the price) it could increase revenue and decrease costs simultaneously

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This strictly increases the profits



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$$\varepsilon_{q,p} < -1$$
, then

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The firm always sets a price that is strictly above marginal cost

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There is a mark-up above marginal cost at the profit maximizing price

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- There is a mark-up above marginal cost at the profit maximizing price
- The amount produced q is below the quantity where p = MC.

 The above analysis already illustrates an important point against monopolies

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 The above analysis already illustrates an important point against monopolies

 Both consumer surplus and total surplus is less than is socially optimal

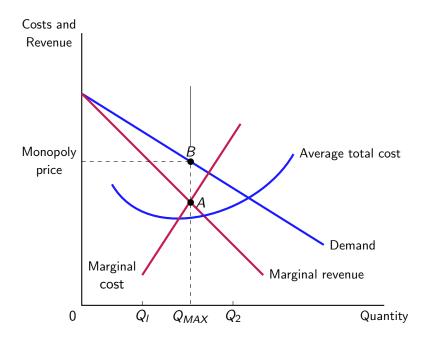
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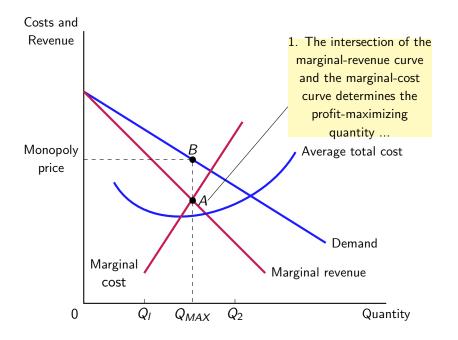
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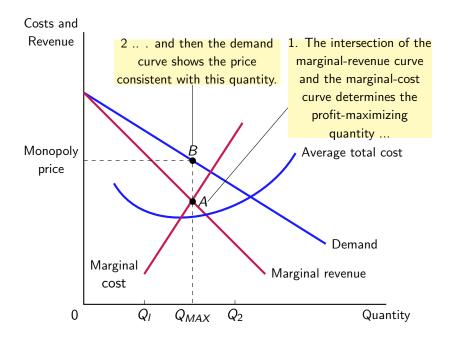
Thus the pricing policies used by monopolies are inefficient, leading to what is called "dead-weight loss"

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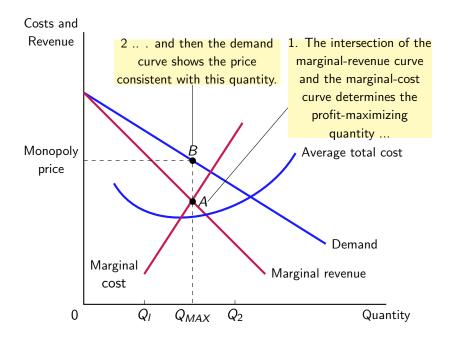


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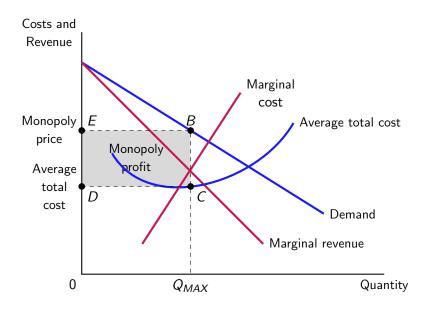


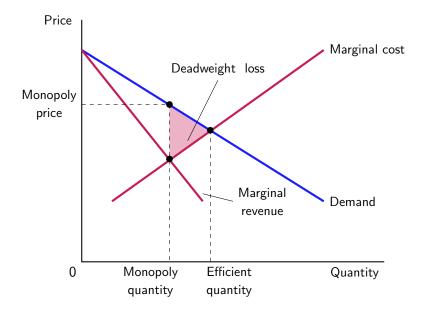


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$$\max_p pq(p) - c(q(p)).$$

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$$\max_p pq(p) - c(q(p)).$$

$$ho=rac{1}{1+rac{1}{arepsilon_{q,p}}}rac{dc}{dq}=rac{1}{1+rac{1}{\kappa}}rac{dc}{dq}.$$

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- If marginal costs are constant at c

$$p = rac{c}{1+rac{1}{\kappa}} \Longrightarrow q(p) = A\left(rac{c}{1+rac{1}{\kappa}}
ight)^{\kappa}$$

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If profits are positive, why aren't more firms entering the market?

Natural monopoly (Microsoft)

Patents

- Political Lobbying: Televisa, Azteca, etc.
- Regulation (Moody and S & P's)
- Demand externalities
 - Classic network externalities (Microsoft): Microsoft Word and Windows are only valuable if a lot of consumers use it.
 - Two-sided markets (Ticketmaster or Uber): consumers value these markets only if there is enough supply of tickets. Similarly suppliers only value these markets if there is demand to meet the supply.