Lecutre 1

Tuesday, January 12, 2021 2:27 PM



Lecture 1: General Equilibrium

Lecture 1: General Equilibrium	
Introduction	
Pure Exchange Economies	
Pareto efficiency	
Edgeworth Box	
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Previous classes

- Consumers behavior (decision theory) was often analyzed separately from firm behavior (producer theory)
- ► When analyzed together, each market was viewed in isolation

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- ▶ When analyzed together, each market was viewed in isolation
- But markets are often intertwined
 - ► Transportation: Uber/metro/ecobici/car
 - Wages across sectors
 - Fruits
 - Beer and tacos

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Example - Fruits

- Suppose that apple and bananas are substitutes
- Supply curve for apples shifts out



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- DD for bananas decreases (exogenous)



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A tour down memory lane

- ▶ Léon Walras started it all (1834-1910)
 - ▶ First to use mathematical tools in economics
 - Supply and demand curves as solutions to a maximization problem
 - Started the "marginal revolution"
- Walras was ultimately after normative questions (is the market economy good?)
- But first, he tackled positive questions (is there an equilibrium? is it unique?)
- Made a lot of progress. In particular came up with "Walras Law": Sum of the values of excess demands across all markets must equal zero always

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- ► What are the properties of such an equilibrium?
 - Is it unique?
 - Is it stable?
 - Is it efficient?

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Pure Exchange Economies

Assume there are
I consumers, I = {1,...,I}
L goods, L = {1,...,L}
Each consumer i is characterized by a utility function uⁱ.
Each consumer can consume goods in x) ∈ ℝ^L₊ → Xi = (Xi, Xi, --, Yi)
Each consumer has an initial endowment of wⁱ ∈ ℝ^L₊.
Each consumer is characterized by the pair (uⁱ, wⁱ).
Assume the utility functions represent neoclassic preferences

Utility functions and neoclassic preferences

A brief reminder

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Utility functions and neoclassic preferences

- A brief reminder
- Utility functions are ordinal not cardinal

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Utility functions and neoclassic preferences

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Utility functions and neoclassic preferences

- A brief reminder
- Utility functions are ordinal not cardinal
- They are used to represent preferences
 - lf $x \succ_i y$ then $u^i(x) > u^i(y)$
 - If f is any increasing function then $f(u^i(x)) > f(u^i(y))$
 - ▶ Hence $f(u^i(\cdot))$ also represents \succ_i
 - $u^i(x) > u^i(y)$ means something, but $u^i(x) u^i(y)$ does not
- ► Neoclassic preferences are well behaved

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X~ LA(X16752) Consonas Predevencios Pure Exchange Economies CONSUNIO AGENTES. Definition (Exchange economy) A pure exchange economy is $\mathcal{E} = \langle \mathcal{I}, (\mathcal{U}, \mathcal{W}) \rangle_{i \in \mathcal{I}} \rangle$ where \mathcal{I} is the set of agents, u^i is a representation of consumer *i*'s preferences and w^i is consumer *i*'s initial endowment. $\omega_i \in \mathbb{R}_{T^{\pm}} \left(\omega_{i, \dots, \omega_i}^{L} \right)$ ► Let be the total endowment of the economy. W = (5, 5)STACOS $\omega = (\omega, \omega)$ An <u>allocation</u> of resources is denoted by $x = (x^1, x^2)$ uss leeves where $x^i \in \mathbb{R}^{L}$ Pure Exchange Economies plansunic AsiGNACIONES Definition (Feasible allocation) The set of *feasible* llocation *F* of an economy $\mathcal{E} = \left\langle \mathcal{I}, (u^{i}, w^{i})_{i \in \mathcal{I}} \right\rangle$ is defined by: $\mathbf{x} = (x^1, x^2, ..., x^l) : x^i \in \mathbb{R}^L_+$ i=1 $\overline{i=1}$ to No "Cites Lecture 1: General Equilibrium Introduction Pure Exchange Economies Pareto efficiency Edgeworth Box 10+10+12+12+ 2 940

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Pareto efficiency			
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Definition (Pareto efficiency)			
Let be an economy. A feasible apocation of resources $x \rightarrow (x^1, x^2,, x')$ is pareto efficient if there isn't another feasible			
allocation $\widehat{X} \neq (\widehat{x}^1, \widehat{x}^2,, \widehat{x}^r)$ such that for every agent i , $u^i(\widehat{x}^i) \ge u^i(x^i)$ and for at least one agent i^* , $u^i^*(\widehat{x}^{i^*}) > u^{i^*}(x^{i^*})$.			
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Pareto efficiency	- L.		
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Definition (Pareto domination)	X ES UN O.F.		
Take two feasible allocations x and x. We say that x Pareto dominates x if for all $i = 1,, I$,	SI NADA FACUBE		
$\underbrace{u_i(\hat{x}_1^i,\ldots,\hat{x}_L^i)}_{i} \ge u_i(x_1^i,\ldots,x_L^i) \qquad \forall \hat{c}$	10 PATOETO DODIAN,	Maurice Q	
and there is at least one consumer j for which		Figure 1	
$u_j(x_1,\ldots,x_L) > u_j(x_1,\ldots,x_L).$		[V= (6300 C, C) Q.L.	
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i ninking about Pareto efficiency	W= 6,500 MXN	7= 1000, 01 7 = 1	(6200, 100, 100, 100, 100, 100, 100, 100,

Thinking about Pareto efficiency

- If x is a Pareto efficient feasible allocation, does it mean that x Pareto dominates all other feasible allocations?
- If there are two allocations (x and y) is it always the case that one Pareto dominates the other?
- For Pareto efficiency, the initial endowments only matter in the sense that they determined the total endowment of the economy
- Social planner should strive to achieve Pareto efficiency at the very least!

Thinking about Pareto efficiency

- If x is a Pareto efficient feasible allocation, does it mean that x Pareto dominates all other feasible allocations?
- If there are two allocations (x and y) is it always the case that one Pareto dominates the other?
- For Pareto efficiency, the initial endowments only matter in the sense that they determined the total endowment of the economy
- Social planner should strive to achieve Pareto efficiency at the very least. However, she may have other concerns such as fairness



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Pareto efficiency	2 CONSULTIDOE
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Edgeworth Box	

$W_{p+H} = W_{p-1}$				
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