

Lecture1

Lecture 1: General Equilibrium

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Lecture 1: General Equilibrium

Introduction

Pure Exchange Economies

Pareto efficiency

Edgeworth Box

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Introduction

Pure Exchange Economies

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Previous classes

- ► Consumers behavior (decision theory) was often analyzed separately from firm behavior (producer theory)
- ▶ When analyzed together, each market was viewed in isolation

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- ▶ When analyzed together, each market was viewed in isolation
- ► But markets are often intertwined

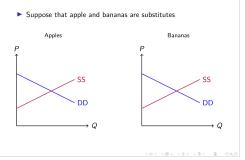
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Previous classes

- ► Consumers behavior (decision theory) was often analyzed separately from firm behavior (producer theory)
- ▶ When analyzed together, each market was viewed in isolation
- ► But markets are often intertwined
 - ► Transportation: Uber/metro/ecobici/car
 - ► Wages across sectors
 - ► Fruits
 - ► Beer and tacos

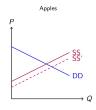
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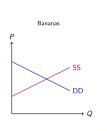




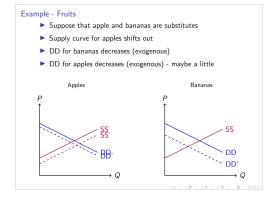


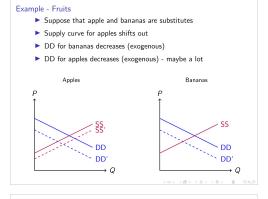
- ▶ Suppose that apple and bananas are substitutes
- ► Supply curve for apples shifts out

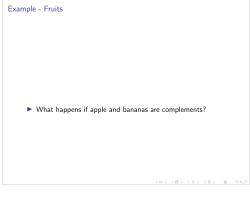




Example - Fruits Suppose that apple and bananas are substitutes Supply curve for apples shifts out DD for bananas decreases (exogenous) Apples Bananas P DD DD DD DD DD Q







A tour down memory lane

- ► Léon Walras started it all (1834-1910)
 - First to use mathematical tools in economics
 - ► Supply and demand curves as solutions to a maximization problem
 - ► Started the "marginal revolution"
- ► Walras was ultimately after normative questions (is the market economy good?)
- ► But first, he tackled positive questions (is there an equilibrium? is it unique?)
- Made a lot of progress. In particular came up with "Walras Law": Sum of the values of excess demands across all markets must equal zero always

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A tour down memory lane

- ▶ Vilfredo Pareto was Walras student (1848-1923)
 - ► Abandoned utilitarianism (i.e., utility functions)
 - ► Embraced "preferences"
 - ▶ Utility functions only have ordinal content
 - ► Comparing "utils" across individuals is meaningless
 - ► (Pareto) optimum/efficiency: Achieved if we can't make someone better-off without making someone worst-off

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A tour down memory lane

- ► Francis Edgeworth (1845 1926)
 - ► Introduced indifference curves
 - ▶ Was the first to ask: Where will voluntary exchange lead to?
 - ► He conjecture his result was aligned with Walras' result

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A tour down memory lane

- ▶ No more advances for a while (until 1950's) then
 - ► Kenneth Arrow
 - ► Gerard Debreu
 - Lionel McKenzie
- Existence
- ► Showed it was Pareto efficient
- ► Two Nobel prizes (Arrow 1972 and Debreu 1974)

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- ► How are goods distributed among consumers?
- ► What incentives are there to exchange goods? What institutions mediate the exchange?
- ► Is there a distribution of goods that leaves everyone satisfied and there aren't any incentives to deviate?

Pure Exchange Economies

- ▶ What are the properties of such an equilibrium?
 - ► Is it unique?
 - ► Is it stable?
 - ► Is it efficient?

Pure Exchange Economies
► Assume there are
▶ I consumers, $\mathcal{I} = \{1,,I\}$
$ ightharpoonup L$ goods, $\mathcal{L}=\{1,,L\}$
▶ Each consumer i is characterized by a utility function u^i .
Each consumer i is characterized by a utility function u^i . Each consumer can consume goods in $x_i \in \mathbb{R}^L_+$
$lackbox{f E}$ Each consumer has an initial endowment of $w^i\in\mathbb{R}_+^L.$
$ ightharpoonup$ Each consumer is characterized by the pair: (u^i,w^i) .
➤ Assume the utility functions represent neoclassic preferences
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Utility functions and neoclassic preferences
► A brief reminder
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Utility functions and neoclassic preferences
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Utility functions and neoclassic preferences
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Utility functions and neoclassic preferences

- A brief reminder
- ▶ Utility functions are ordinal not cardinal
- ▶ They are used to represent preferences
 - ▶ If $x \succ_i y$ then $u^i(x) > u^i(y)$
 - ▶ If f is any increasing function then $f(u^i(x)) > f(u^i(y))$
 - ▶ Hence f(uⁱ(·)) also represents >_i
 - lacksquare $u^i(x)>u^i(y)$ means something, but $u^i(x)-u^i(y)$ does not
- ► Neoclassic preferences are well behaved

U(x) = x3y2 (n(u(xy))=3(nx+2hy

Utility functions and neoclassic preferences

- A brief reminder
- ► Utility functions are ordinal not cardinal
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 - If f is any increasing function then $f(u^i(x)) > f(u^i(y))$
 - ▶ Hence $f(u^i(\cdot))$ also represents \succ_i
 - $u^i(x) > u^i(y)$ means something, but $u^i(x) u^i(y)$ does not
- ► Neoclassic preferences are well behaved
 - $\,\blacktriangleright\,$ They can be represented by a utility function
 - ► They are weakly monotonic
 - ► They are quasi-concave

Pure Exchange Economies

Definition (Exchange economy)

A pure exchange economy is $\mathcal{E} = \left\langle \mathcal{I}, \left(u^i, w^i\right)_{i \in \mathcal{I}} \right\rangle$ where \mathcal{I} is the set of agents, u^i is a representation of consumer i's preferences and w^i is consumer i's initial endowment.

- Let $w = \sum_{i=1}^{J} w^i$ be the total endowment of the economy.
- An allocation of resources is denoted by $x=(x^1,x^2,...,x^l)$ \mathbb{R}^{L} \mathbb{R}^{L} where $x^i \in \mathbb{R}^{L}_+$.

Pure Exchange Economies

Definition (Feasible allocation)

The set of *feasible* allocation F of an economy $\mathcal{E} = \left\langle \mathcal{I}, \left(u^i, w^i \right)_{i \in \mathcal{I}} \right\rangle$ is defined by:

$$F = \left\{ x = (x^1, x^2, ..., x^l) : x^i \in \mathbb{R}^L_+, \sum_{i=1}^l x^i = \sum_{i=1}^l w^i \right\}$$

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Pareto efficiency

Pareto efficiency

Definition (Pareto efficiency) Let $\mathcal E$ be an economy. A feasible allocation of resources $x=(x^1,x^2,...,x^I)$ is Pareto efficient if there isn't another feasible allocation $\widehat x=(\widehat x^1,\widehat x^2,...,\widehat x^I)$ such that for every agent $i,u^i(\widehat x^i)\geq u^i(x^I)$ and for at least one agent $i^*,u^i(\widehat x^{i'})>u^i^*(x^{i*})$.

Pareto efficiency

Definition (Pareto domination)

Take two feasible allocations x and \hat{x} . We say that \hat{x} Pareto dominates x if for all $i=1,\ldots,I$,

$$u_i(\hat{x}_1^i,\dots,\hat{x}_L^i) \geq u_i(x_1^i,\dots,x_L^i)$$

and there is at least one consumer \boldsymbol{j} for which

$$u_j(\hat{x}_1^j,\ldots,\hat{x}_L^j)>u_j(x_1^j,\ldots,x_L^j).$$

Thinking about Pareto efficiency

- ► If x is a Pareto efficient feasible allocation, does it mean that x Pareto dominates all other feasible allocations?
- ► If there are two allocations (x and y) is it always the case that one Pareto dominates the other?
- ► For Pareto efficiency, the initial endowments only matter in the sense that they determined the total endowment of the economy
- ► Social planner should strive to achieve Pareto efficiency at the very least!

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Thinking about Pareto efficiency

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- ▶ If there are two allocations (x and y) is it always the case that one Pareto dominates the other?
- ► For Pareto efficiency, the initial endowments only matter in the sense that they determined the total endowment of the economy
- ► Social planner should strive to achieve Pareto efficiency at the very least! However, she may have other concerns such as fairness.

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Thinking about Pareto efficiency

- ▶ If utility is strictly increasing, then can a Pareto efficient allocation be such that $\sum_{i=1}^{l} x_j^i < \sum_{i=1}^{l} w_j^i$?
- ► The set of all Pareto allocations is known as the contract

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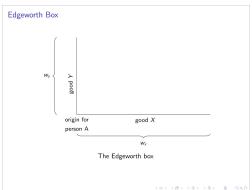
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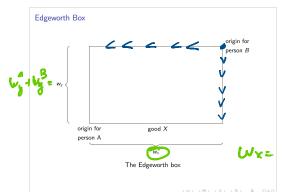
Pareto efficiency

Edgeworth Box

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Wx + WxB

