Lecture6

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Lecture 6: General Equilibrium

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Lecture 6: General Equilibrium

A few things I forgot to say about economies with production

Robinson Crusoe

Two firms

General Economies with Many Consumers and Production



Lecture 6: General Equilibrium

A few things I forgot to say about economies with production

Robinson Crusos

Two firms

General Economies with Many Consumers and Production



- ► With production, Edgeworth box illustrations are no longer helpful
- ► Depending on the production plan, the size of the box can change
- ► Instead we work with what is called a production possibilities frontier



Lecture 6: General Equilibrium

A few things I forgot to say about economies with production

Robinson Crusoe

Two fire

General Economies with Many Consumers and Production



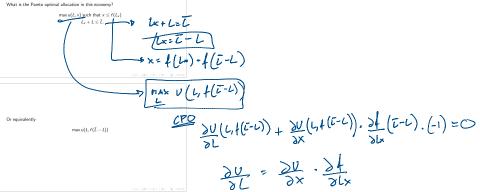
Lecture 6: General Equilibrium Robinson Crusoe ► Imagine the problem of Robinson Crusoe, living alone in an island. He is the only producer and the only consumer

Suppose that the consumer (Robinson) has a utility function:

where \boldsymbol{x} are coconuts. There is one firm (Robinson) that can convert labor to coconuts:

The endowment is $(0, \bar{L})$

What is the Pareto optimal allocation in this economy?



 $\max u(L, f(\bar{L} - L))$

We can solve this either using calculus or graphically

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Using calculus...

Using calculus... This is the order condition:

$$\frac{\partial u}{\partial L}(L, f(\tilde{L}-L)) - \frac{\partial u}{\partial x}(L, f(\tilde{L}-L)))f'(\tilde{L}-L) = 0$$

Using calculus... This is the order condition:

 $\frac{\partial u}{\partial L}(L,f(\bar{L}-L)) - \frac{\partial u}{\partial x}(L,f(\bar{L}-L)))f'(\bar{L}-L) = 0$

$$\frac{\partial u}{\partial L}(L, f(\bar{L} - L)) = \frac{\partial u}{\partial x}(L, f(\bar{L} - L)))f'(\bar{L} - L)$$

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$$\frac{\partial u}{\partial L}(L, f(\bar{L} - L)) = \frac{\partial u}{\partial x}(L, f(\bar{L} - L)))f'(\bar{L} - L)$$

$$\frac{\partial \omega}{\partial L}(L, f(\overline{L} - L))$$

 $\frac{\partial \omega}{\partial x}(L, f(\overline{L} - L))) = f'(\overline{L} - L)$

$$f'(\bar{L} - L) = \frac{\partial u}{\partial L}(L, f(\bar{L} - L)) = MRS_{L,x}$$

▶ If Robinson gives up 1 unit of consumption in L, $f'(\bar{L}-L)$ describes how much more in terms of x Robinson will be able to consume

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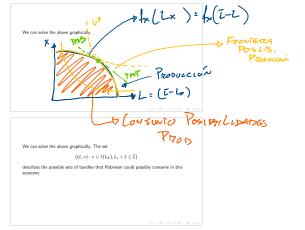
- ▶ If Robinson gives up 1 unit of consumption in L, $f'(\bar{L}-L)$ describes how much more in terms of x Robinson will be able to consume
- \blacktriangleright This is what is called a Marginal Rate of Transformation of good L to x

$$f'(\bar{L} - L) = \frac{\frac{\partial u}{\partial \bar{L}}(L, f(\bar{L} - L))}{\frac{\partial u}{\partial L}(L, f(\bar{L} - L))} = MRS_{L,x}$$

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$$\begin{split} f'(\bar{L}-L) &= \frac{\frac{\partial u}{\partial L}(L, f(\bar{L}-L))}{\frac{\partial u}{\partial x}(L, f(\bar{L}-L))} = MRS_{L,x} \\ &MRT_{L,x} = MRS_{L,x}. \end{split}$$

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We can solve the above graphically. The set $\{(L, x) : x \leq f(L_X), L_X + L \leq \tilde{L}\}$ describes the possible sets of bundles that Robinson could possibly consume in this economy. This is called the ${\bf production\ possibilities\ set\ (PPS)}$ We can solve the above graphically. The set

 $\{(L, x) : x \le f(L_X), L_x + L \le \bar{L}\}$

describes the possible sets of bundles that Robinson could possibly consume in this economy.

This is called the production possibilities set (PPS)

The boundary of the PPS is theproduction possibilities frontier (PPF)

The frontier is basically described by the curve:

 $x = f(L_x), L_x \in [0, \overline{L}].$

The frontier is basically described by the curve:

 $x = f(L_x), L_x \in [0, \overline{L}].$

The maximization problem for finding Pareto efficient allocations simply amounts to maximizing the utility of Robinson subject to being inside this constraint set.

Lecture 6: General Equilibrium

Robinson Crusoe Econ 1 Intuition

- ightharpoonup Recall that at a Pareto optimum, we found that we must have $MRT_{L,x} = MRS_{L,x}$
- \blacktriangleright Suppose one is at an allocation where $\textit{MRT}_{L,\times}=2>\textit{MRS}_{L,\times}=1$
- ► Such an allocation cannot be a Pareto efficient allocation. Why?



 \blacktriangleright Recall that at a Pareto optimum, we found that we must have $\textit{MRT}_{L,\times} = \textit{MRS}_{L,\times}$ ightharpoonup Suppose one is at an allocation where $MRT_{L,x}=2>MRS_{L,x}=1$ ► Such an allocation cannot be a Pareto efficient allocation. Why? One could potentially reorganize production to get an even better outcome for the consumer Lecture 6: General Equilibrium A few things I forgot to say about economies with production Robinson Crusoe Two firms General Economies with Many Consumers and Production

Lecture 6: General Equilibrium

Two firms



- ► The consumer has a utility function u(x, y)
- ► The consumer is endowed with 0 units of both x and y but x and y can be produced from labor and capital
- \blacktriangleright She is endowed with K units of capital and L units of labor
- \blacktriangleright There are two firms each of which produces a commodity x and y.
- Firm x produces x according to a production function f_x and firm y produces y according to a production function f_y:

 $f_x(\ell_x, k_x), f_y(\ell_y, k_y).$

To solve for the Pareto efficient allocation we solve:

 $\max u(x, y)$ such that $x \le f_x(\ell_x, k_x), y \le f_y(\ell_y, k_y),$ $L \ge \ell_x + \ell_y, K \ge k_x + k_y.$



Lecture 6: General Equilibrium

Two firms Graphical Approach





 $\{(x, y) : x \le f_x(\ell_x, k_x), y \le f_y(\ell_x^A, k_y), \ell_x + \ell_y \le L, k_x + k_y \le K\}.$



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Then given the PPS, we want to maximize the utility of the agent subject to being inside the PPS. If we want to maximize the utility of the agent, we need:

- 1. The chosen (x^*, y^*) must be on the PPF.
- 2. The indifference curve of the consumer must be tangent to the PPF at (x^*,y^*) .

Lecture 6: General Equilibrium

A few things I forgot to say about economies with production

Robinson Crusoe Econ 1 Intuition

Two firms

Graphical Approach Calculus Approach

General Economies with Many Consumers a

Solving the Maximization Problem

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To find the PPF: given that x units of commodity x must be produced, what is the maximum amount of y's that can be produced?

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To find the PPF: given that x units of commodity x must be produced, what is the maximum amount of y's that can be produced? Thus

 $PPF(x) = \max_{\ell_y, k_y} f_y(\ell_y, k_y)$ such that $x = f_x(L - \ell_y, K - k_y)$.

Setting up the Lagrangian we get:

 $\max_{\ell_y, k_y} f_y(\ell_y, k_y) + \lambda (f_x(L - \ell_y, K - k_y) - \overline{x}))$

The first order conditions give us:

$$\begin{split} &\frac{\partial f_y}{\partial \ell}(\ell_y^*,k_y^*) - \lambda \frac{\partial f_x}{\partial \ell}(L-\ell_y^*,K-k_y^*) = 0 \\ &\frac{\partial f_y}{\partial k}(\ell_y^*,k_y^*) - \lambda \frac{\partial f_x}{\partial k}(L-\ell_y^*,K-k_y^*) = 0 \end{split}$$

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$$\begin{split} \frac{\partial f_y}{\partial \ell} (\ell_y^*, k_y^*) &= \lambda \frac{\partial f_x}{\partial \ell} (L - \ell_y^*, K - k_y^*) \\ \frac{\partial f_y}{\partial k} (\ell_y^*, k_y^*) &= \lambda \frac{\partial f_x}{\partial k} (L - \ell_y^*, K - k_y^*) \end{split}$$

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Thus at the optimum, we have:

$$TRS_{\ell,k}^{y} = \frac{\frac{\partial f_{\ell}}{\partial \ell}(\ell_{y}^{u}, k_{y}^{u})}{\frac{\partial f_{\ell}}{\partial \ell}(\ell_{y}^{u}, k_{y}^{u})} = \frac{\frac{\partial f_{\ell}}{\partial \ell}(L - \ell_{y}^{u}, K - k_{y}^{u})}{\frac{\partial f_{\ell}}{\partial k}(L - \ell_{y}^{u}, K - k_{y}^{u})} = TRS_{\ell,k}^{x}.$$

- ▶ To actually solve for the optimal x^* and y^* we plug this back into the constraint $x=f_s(L-\ell_s^*,K-k_s^*)$
- ▶ Therefore at a Pareto optimum we must have TRS^x_{I,k} = TRS^x_{I,k} equalized
- $\,\blacktriangleright\,$ You should be able to come up with the Econ 1 intuition for this as we have done previously

- ▶ A Pareto optimum also requires bullet point 2 above (i.e., indifference curve is tangent to PPF)
- ► The slope of the indifference curve is given by:

$$-MRS_{x,y} = -\frac{\partial u}{\partial x}(x^*, y^*)$$

➤ What is the slope of the PPF?

- ➤ Note that mathematically, this is given by PPF'(x)

 ➤ How do we calculate that?
 - $PPF(x) = \max_{\ell_y, k_y} f_y(\ell_y, k_y) + \lambda (f_x(L \ell_y, K k_y) x))$

$$PPF(x) = \max_{\ell_y, k_y} r_y(\ell_y, \kappa_y) + \lambda (r_x(L - \ell_y, K - \kappa_y) - x)$$

► By the envelope theorem

$$\begin{split} PPF'(x) &= & -\lambda \\ &= & \frac{\frac{\partial f}{\partial t}(\ell_j^*, k_j^*)}{\frac{\partial f}{\partial t}(L - \ell_j^*, K - k_j^*)} \\ &= & -\frac{\frac{\partial f}{\partial t}(\ell_j^*, k_j^*)}{\frac{\partial f}{\partial t}(L - \ell_j^*, K - k_j^*)} \\ &= & -MRT_{x,y} \end{split}$$

Note that mathematically, this is given by PPF'(x)
How do we calculate that?

 $PPF(x) = \max_{\ell_y, k_y} f_y(\ell_y, k_y) + \lambda (f_x(L - \ell_y, K - k_y) - x))$

PPF'(x) =

 $-\frac{\frac{\partial f_r}{\partial t}(\ell_f^*, k_f^*)}{\frac{\partial f_r}{\partial t}(L - \ell_f^*, K - k_f^*)}$ $-\frac{\frac{\partial f_r}{\partial k}(\ell_f^*, k_f^*)}{\frac{\partial f_r}{\partial k}(L - \ell_f^*, K - k_f^*)}$

► Therefore, at a Pareto optimum:

 $MRT_{x,y} = MRS_{x,y}$.

Thus we have learned the following: A Pareto efficient allocation is characterized by two conditions:

1. (x^*, y^*) is on the PPE; $TRS_{\ell,k}^x = TRS_{\ell,k}^y$.

2. At (x^*,y^*) the indifference curve is tangent to the PPF: $MRS_{x,y} = MRT_{x,y}$.

Lecture 6: General Equilibrium

Two firms

Calculus Approach II

We solve directly the original maximization problem.

max u(x, y) such that $x \le f_x(\ell_x, k_x), y \le f_y(\ell_y, k_y),$ $L \ge \ell_x + \ell_y, K \ge k_x + k_y$

L= Lx+Ly K= Kerky

3×3k+3y, 3k (-1)=0

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We can simplify the problem:

 $\max_{\ell_x, k_x} u(f_x(\ell_x, k_x), f_y(L - \ell_x, K - k_x))$

Then the first order conditions give us:

$$\begin{split} &\frac{\partial u}{\partial x} \left(f_{i}(f_{i}^{a}, k_{i}^{a}), f_{j}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial f_{i}}{\partial t} \left(f_{i}^{a}, k_{j}^{a} \right) - \frac{\partial u}{\partial y} \left(f_{i}(f_{i}^{a}, k_{j}^{a}), f_{j}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial f_{j}}{\partial t} \left(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a} \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}(f_{i}^{a}, k_{j}^{a}), f_{j}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial f_{j}}{\partial t} \left(f_{i}^{a}, k_{j}^{a} \right), f_{j}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \frac{\partial f_{j}}{\partial t} \left(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a} \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial f_{j}}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial f_{j}}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial f}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, k_{j}^{a}, h_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \frac{\partial u}{\partial t} \left(f_{i}^{a}, h_{j}^{a}, h_{j}^{a}, h_{j}^{a}(\mathbf{L} - I_{i}^{a}, K - k_{j}^{a}) \right) \\ &\frac{\partial u}{\partial t} \left(f_{i}^{a}, h_{j}^{a}, h_{j}^{a$$

Then the first order conditions give us:

 $\frac{\partial u}{\partial x} (f_{x}(\ell_{x}^{x}, k_{x}^{x}), \ell_{y}(\mathbf{L} - \ell_{x}^{x}, K - k_{x}^{x})) \frac{\partial f_{x}}{\partial y} (\ell_{x}^{x}, k_{x}^{x}) - \frac{\partial u}{\partial y} (f_{x}(\ell_{x}^{x}, k_{x}^{x}), \ell_{y}(\mathbf{L} - \ell_{x}^{x}, K - k_{x}^{x})) \frac{\partial f_{y}}{\partial y} (\mathbf{L} - \ell_{x}^{x}, K - k_{x}^{x}) = 0,$

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A few things I forget to say ahout economies with production
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Rations Crown
A concrete example
Two firms
Gapheal Approach
Calcular Approach
Calcular Approach
Calcular Approach
Concrete Example

Lecture 6: General Equilibrium

 $TRS_{\ell,k}^x = TRS_{\ell,k}^y,$ $MRS_{x,y} = MRT_{x,y},$

Seneral Economies with Many Consumers and Production Solving the Maximization Problem

Suppose that the utility function are given by: $u(x,y)=\sqrt{sy}$ and suppose that the production functions are given by: $f_{k}(\ell_{x},k_{x})=\sqrt{\ell_{x}k_{x}},f_{y}(\ell_{y},k_{y})=\sqrt{\ell_{y}k_{y}}.$

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Approach 1: First lets characterize the PPF. $PPF(x) = \max f_y(L - \ell_x, K - k_y) \text{ such that } f_x(\ell_x, k_y) = x.$

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By the first order condition, we need:

 $\begin{array}{l}
\text{FPP}(\bar{k}) = \max_{k_{1}k_{2}} \frac{(\bar{k} - k_{2})^{1/2}}{\ell_{3}} \sin \left(\frac{k_{1}k_{2}}{k_{2}} \right)^{2} \sin \left(\frac{k_{1}k_{2}}{k_{2}k_{2}} \right)^{2} \\
\text{If } (\bar{k} - k_{2})^{1/2} \cdot \left(\bar{k} - k_{2} \right)^{1/2} + \lambda \left(\bar{k} - k_{1}k_{2} \right)^{2} \\
\frac{\partial f}{\partial k_{2}} = \frac{1}{2} (\bar{k} - k_{2})^{1/2} \left(-1 \right) \left(\bar{k} - k_{2} \right)^{1/2} - \lambda \frac{1}{2} k_{2} k_{1} - 0 \\
\frac{\partial f}{\partial k_{2}} = \frac{1}{2} \left(\bar{k} - k_{2} \right)^{1/2} \left(\bar{k} - k_{2} \right)^{1/2} \left(-1 \right) - \lambda \frac{1}{2} k_{1} k_{2} - 0 \\
\frac{\partial f}{\partial k_{2}} = \frac{1}{2} \left(\bar{k} - k_{2} \right)^{1/2} \left(\bar{k} - k_{2} \right)^{1/2} \left(-1 \right) - \lambda \frac{1}{2} k_{2} k_{2} - 0 \\
\frac{\partial f}{\partial k_{2}} = \frac{1}{2} \left(\bar{k} - k_{2} \right)^{1/2} \left(\bar{k} - k_{2} \right)^{1/2} \left(-1 \right) - \lambda \frac{1}{2} k_{2} k_{2} - 0 \\
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\frac{\partial f}{\partial k_{2}} = \frac{1}{2} \left(\bar{k} - k_{2} \right)^{1/2} \left(\bar{k} - k_{2} \right)^{1/2} \left(\bar{k} - k_{2} \right)^{1/2} \left(-1 \right) - \lambda \frac{1}{2} k_{2} k_{2} + 0 \\
\frac{\partial f}{\partial k_{2}} = \frac{1}{2} \left(\bar{k} - k_{2} \right)^{1/2} \left($

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By the first order condition, we need:

$$\frac{k_x^*}{\ell_x^*} = \frac{\frac{\partial \ell_x}{\partial t}(\ell_x^*, k_x^*)}{\frac{\partial \ell_x}{\partial t}(\ell_x^*, k_x^*)} = \frac{\frac{\partial \ell_x}{\partial t}(L - \ell_x^*, K - k_x^*)}{\frac{\partial \ell_x}{\partial t}(L - \ell_x^*, K - k_x^*)} = \frac{K - k_x^*}{L - \ell_x^*} \Longrightarrow k_x^* = \frac{K}{L}\ell_x^*.$$

Plug this back into the constraint:

$$f_x(\ell_x^*, k_x^*) = x \Longrightarrow \sqrt{\ell_x k_x} = x \Longrightarrow \ell_x^* = \sqrt{\frac{L}{K}}x.$$

Therefore

$$f_{y}(L - \ell_{x}, K - k_{x}) = y$$

$$\sqrt{\left(L - \sqrt{\frac{L}{K}}x\right)\left(K - \sqrt{\frac{K}{L}}x\right)} = y$$

$$PPF(x) = \left(\sqrt{KL} - x\right)$$

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Then we need to maximize the following:

 $\max_{x,y} \sqrt{xy} \text{ such that } y = \sqrt{KL} - x.$

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The Pareto efficient allocation is given by:

$$\left(x^* = y^* = \frac{1}{2}\sqrt{KL}, \ell_x^* = \ell_y^* = \frac{1}{2}L, k_x^* = k_y^* = \frac{1}{2}K\right).$$

Lecture 6: General Equilibrium

A few things I forgot to say about economies with production

Robinson Crusoe

Two firm

General Economies with Many Consumers and Production

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Lecture 6: General Equilibrium

34 . 1 ([-lx) " ([-kx)" (-1) -) 1 (x kx 2 c) \frac{\frac{1}{\ille{\(\beta\)}^{1/2}} \left(\beta\) \left K-Kx = Kx Klx-Kxtx= KxI-Kxtx y= (I-Lx)1/2 (R-Kx)1/2 = (1-Lx) 1/2 (1-Lx) 1/2

Lecture 6: General Equilibrium

General Economies with Many Consumers and Production

The set of Pareto efficient allocations will be characterized by the following

$$\max_{(s,s)} u_1(x_1^1, x_2^1, \dots, x_L^1) \text{ such that } u_2(x_1^2, \dots, x_L^2) \ge \underline{u}_2 = u_2(\hat{x}_1^2, \dots, \hat{x}_L^2),$$

$$\begin{split} &m(s_1^i,\dots,s_\ell^i) \geq \underline{w}_i = m(\tilde{s}_1^i,\dots,\tilde{s}_\ell^i),\\ &x_1^i+\dots s_1^i+\tilde{s}_1^i+\dots+\tilde{s}_\ell^i \leq \sum_{j'\in[i]-1} b_j(z_j^i,\dots,z_\ell^i) + \sum_{i=1}^j \omega_j^i,\\ &\vdots\\ &x_1^i+\dots x_\ell^i+\tilde{s}_\ell^i+\dots+\tilde{s}_\ell^i \leq \sum_{j'\in[i]} b_j(z_j^i,\dots,z_\ell^i) + \sum_{j'} \omega_j^i. \end{split}$$

Lecture 6: General Equilibrium

General Economies with Many Consumers and Production Solving the Maximization Problem

$$\frac{\partial a_1}{\partial x_1}(k_1^1, \dots, k_1^l) = \frac{\partial a_2}{\partial x_1}(k_1^2, \dots, k_1^2) = \dots = \frac{\partial a_k}{\partial x_k}(k_1^1, \dots, k_1^l)$$

$$\frac{\partial z_{i^{\prime\prime}}}{\partial l_{i^{\prime\prime}}}(z_{1}^{\prime\prime}, \dots, z_{L}^{\prime\prime}) = \frac{\partial z_{i^{\prime\prime}}}{\partial z_{i^{\prime\prime}}}(\hat{z}_{1}^{\prime\prime}, \dots, \hat{z}_{L}^{\prime\prime}) = \dots = \frac{\partial z_{i^{\prime\prime}}}{\partial z_{i^{\prime\prime}}}(\hat{z}_{1}^{\prime\prime}, \dots, \hat{z}_{L}^{\prime\prime})$$

Txy S.a. y=1-X y = xy + x (y2-1+x)

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